

### Problem of the week #3

Due February 7th

Define  $p_{ij}$  to be one of the six minors of a matrix  $M$ :

$$M = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 \\ y_1 & y_2 & y_3 & y_4 \end{bmatrix}, \quad p_{ij} = \det \begin{bmatrix} x_i & x_j \\ y_i & y_j \end{bmatrix}.$$

**Problem.** Find a (nontrivial) polynomial equation valid for all  $M$ :

$$Q(p_{12}, p_{13}, p_{14}, p_{23}, p_{34}, p_{24}) = 0.$$

*Hint.* The expression  $Q$  involves each  $p_{ij}$  exactly once.

- Partial credit may be given for partial answers.
- Each POW will be due the following week at 1pm.
- Questions? Email: [bthorner@unomaha.edu](mailto:bthorner@unomaha.edu)
- Submit solutions to (above email), DSC 210, or DSC 203.
- POWs, solutions, backgrounds, leaderboard available at

[https://www.unomaha.edu/college-of-arts-and-sciences/mathematics/student-opportunities/pow\\_solutions.php](https://www.unomaha.edu/college-of-arts-and-sciences/mathematics/student-opportunities/pow_solutions.php)